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## ABSTRACT

This study assessed the effectiveness of the remedial/developmental mathematics program developed at Ramapo College of New Jersey. Data was gathered from a random sample of 604 students who participated in the program for at least part of the three-year period 1981-84 and for whom both pretest and posttest scores were zuailable in at leasf. One skill area (computation or algebra). The New Jersey College Basic Skills Placement Test was used, with 30 computation items and 30 algebra items. Significant differences were found between pre- and posttest scores over the three-year period, for bath computation and algebra. Over 72 percent of the students enrolled in the remedial/developmental courses successfully completed them. Furthermore, the findings indicated that the program contributed significantly to the improvement of students' mathematics skills and that they retained a great deal of the content iearned. Students successfully completing the prog:am appeared to have the same cppcrtunity for success in subsequent mathematics courses as did students not requiring remediation. (MNS)

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Gabriella Wepner .
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The purposi of this study was to assess the effectiveness of the remedial/developmental mathematics program developed at'Ramapo College of New Jersey, a four year state college arc to show that mathematics remediation can be highly successful as evidenced by an expost facto evaluation of the program. .

## Perspective

For years, colleges throughout the country iave been struggling with various degrees of success to address the ingdequacy of mathematical skills brought to postsecondary incti-dtions by entering freshmen ánd refirning adij" students. Although almont every college and university in the nation offers some type of remediation in mathematics, assessments of these remedial efforts have been relatively imprecise. Generally, there, have 'been vague descriptions of prógr'am evaluation procedures and the results quoted have been' in terms of the number or percentage of students süccessfully completing the remedial process.

- The primáry aim of postsecondary mathematics remediation is to : ufficiently, improve the mathematical skills of remedial students so they can successfully complete college level mathematics or mathematics dependent courses. The expectation is that successful remediation will allow the same opportunity of success to remedial students as is available to students
not requiring remediation.
Given the huge number cf students demonstrating mathematical skill deficiencies; successful mathematics remediation becones crucial for, the maintenance of a viable pool of students who can chonse the more technically or mathematically oriented fields needed in our society.

Unfortunately, despite the proifferation of large scale remedial mathematics programs and their concimmitant, high costs both to institutions and to the students involved, there has been little concrete evidence to affirm that máthematics remediation on the college level is actually successful in achieving its purpose. In order to provide such evidence, program evaluations must. address. questions such as:

1. How much of an improvement is demonstrated'by students in the program?
2. Are pragram results consistent over time?
3. Was the instruction provided responsible for student progress or did. maturation or other work in college lead to improved student mathematical skill performance.. .
4. Do students remember what they learned in the program?
5. How well do remedial/developmental students fare - in comparisoi to non-remedial/developmental students in other mathematics courses?

Objectives

In order, to provide answers to the frevious" question, the specific objectives of the study were to determine the

## following:

! $1 . \quad$ Do significant differences exist between the
pre-instructional. skills assessment of students in remedial/de-
velopmental mathematics courses and their post-instructional
skills, assessment?
2. Are these differences, consistent, i.e. does the program achieve similar results each year?
3. Does the remedial/fevelopmentel mathematics instruction provided significiantly contribute to the improvement of student mathematical skills?
4. Do students who have participated in the program demonstrate retention of content over time?
5. Do students successfully completing the remedial and/or de'velopmental courses demonstrate similar achievement when compared to non remedial/nondevelopmental students in the same subsequent mathematics courses.

Procedures

## Data Source

To achieve the objectives of the study, data was gathered on a random sample of 604 remedial/developmental students who participated in the program during at least part of the three year period 1981-1984 and for whom both pretest anc postest sçores werer:available in at.least one skill.area. The data collectad consisted of placement, scores, pretest scores and posttest sco.es in computation and algebra. The
instruments used for all testing were alternate forms of the New - Jersey College Basic Skills Placement Test (NJCBSPT), Computation and/or, Algebra sections.

The NJCBSFT is user to assess student basic skills competencies by the entire state college system and also by many independent New Jersey colleges and universities. The Computation section consists of 30 multiple choice questions dealing with fractions, decimals, percent and simple arithmetic type word problems. The" content is limited to elementary school topics. The Algebra section also consists of 30 multiple choice questions dealing with elementary algebra. Content ic comparable to topics covered in secondary school first-year algebra courses. The validity and reliability for this instrument has been established through the auspices of the Educational Testing Service (ETS), Princeton, New Jersey.

The New Jersey College Basic Skills Placement Test is administered to all entering ${ }^{\text {Freshmen }}$ upon admission to college, usually during the summer months prior to the Fall semester. The results are, used to determine appropriate placement of students into remedial, developmental or college-level courses. Not 'all students, however, enroll in the required courses immediately.

Placement criteria at Ramapo College are as follows:

- 1. Remedial Course (BCM') - computation score of les's than 1 " 6 out of 30 correct.

The remedial course emphasizes computational skills and pre-algebra skills.
2. Development Course (ICM) - computation score between

16 and 21 correct out of 30 , algebra score less than 15 out 30 correct. :
3. Developmental course (IM) - computation score greater than 21 out of 30 correct and algebra score less than 21 correct out of 30 .

Both deveḷopmental courses emphasize elementary algebra skills
4. College-level course (College Algebra) - algebra score greater than 21 out of 30 correct.

Placement score data for this study consisted of the results of the initial placement testing administered during the Spring and Summer of $1981, \quad$ ' 82 , ' 83 , and ' 84.

The pretest data for the study consisted of scores achieved on a form of the NJCBSPT administered during the first week of classes to students enrolled in" program courses (remedial and/or developmental classes) and in the College Algebra classes. This testing was also the data source for measuring retention of content learned, since a student successfully completing the remedial and/or developmental course who enrolled in the subsequent developmental churse or College Algebra course was pretested in that course -a semester or more lat?r.

Posttest data consisted of scores achieved on an alternate form of the NJCBSPT administered during the last week of classes in each course, each semester. Remedial (BCM) students were posttested in computation orly. Developmental (ICM or IM) students were posttested in Computation and Algebra.

The data source for evaluating success in college-level
mai metics courses consisted of final grades received in College Algebra classes in which at least five former remedial/developmentalstudents were enrolled. Thus there were 130 non-remedial/developmental students a. 75 former remedial/developmental ${ }^{\text {/ }}$ students in this sample.

## Methods

To achieve the objectives of the study an ex post fact analysis of data was conducted for a three year period 1981-1984. 604 remedial and/or developmental students, who participated in the program for at least part of the three year period (1981-1984) were randomly selected. Pretest, posttest, and placement data were collected and analyzed according to the specifically stated objectives of the study.

1. In order to determine if significant differences , existed between the pre-instructional skills assessment of students enrolled in remedial/developmental mathematics and their post-instructional skills assessment, pretest scores in computation were compared to post test scores in computation for remedial students and pretest scores in computation and algebra were compared to respective posttest scores for developmental students.
$\gamma^{\text {. }}$ To determine if the differences between pretest and posttest scores were consistent over time, these scores were compared by skill area, and course level, each semester, for each academic year 1981-1984.
2. As this was an ex post factor study it was impossible
to use an experimental design with experimental/control.groups to show that the program's instructional activities were clearly responsible for the improved mathematical skills performance of the students in the program. Consequently an alternative eveluation design was implemented to determine if the remedial/developmental program activities significantly contributed to the improvement of student mathematical skilhs. Placement, pretest, and posttest data for students who initially enrolled in the college at the same time were analyzed.

From the initial group of 604 students, data for 164 students who first enrolled at the college in Fall 1983 was grouped according to those students who enrolled in remedial/developmental fourses in Fall '83 (first semester) and those who waited until Spring ' 84 (second semester) to enroll in remedial/developmental courses. This population was chosen since the largest.group in the random sample was from 1983-84 academic year. Comparisons were as follows:
a) Initial placement scores of students who enrolied in remedial or developmental courses. in their first semester were compared to the initial. placement scores of students. who enrolled in remedial or developmental courses in their sectond semester. This comparison was conducted to ensure the comparability of the two groups on this measure for initial mathematical skill ability.
b) Pretest scores for students enrolled in their first semester were compared to the pretest scores of students enrolled in their second semester in the same course. The assumption here was that, if factors such as maturation, exposure
to other college courses, tesf taking experience, etc., contributed to improved mathematical skill performance, then -students taking the pretest in Spring 'g't should score significantly higher than students who were pretested in Fall '83 given' no significant dífferences in`initig1 placement. scores.
c) Posttest scores for students enrolled in their first eemester were, compared to posttest scores for students enrolled the second semester in the same course. The assumption here was that if factors other than program activities contributed significantly to improved mathematical skills performance then Spring ' 84 posttest scor ss' should be significantly'higher than Fall ' 83 postest scores because of the extended exposure time to such factors available to second semester students.

- d) Pretest scores and posttest scores were compared for those students who enrolled in the remedial or developmental course during their first, semester. Pretest scores of students enrolled in their second semester were compared to postiest scores of students enrolied in the first semester. The assumption here was that if factors unrelated to the program's activities contributed significantly to the improvement of student mathematical skills then the differences between first semester posttest scores and scond semester pretest scores should not be as significant as the difference between first semester pretest scores and first semester posttest scores.

4. To determine if students who participated in the program could demonsirate retention of content, initial pretest scores in computation and algebra were rompared to respective
retention test scores achieved at least one semester later during subsequent course, pretesting. " Posttest scores achieved at the end of instruction in computation and algebra were compared to respective retention test scores achieved at least one semester later in subsequent course pretesting. of the ${ }^{\circ}$ original 604 students in the sample there were 85 students for whom pretest, posttest and retention (pretest) data were available in computation ind 115 students for whom both pretest, and posttest and retention test data were available in algebra. College policy.allowed remedial students over a year's time to entoll in subsequent developmental courses and developmental students over two year's time to fulfill thel Collyege Algebra requirement, thus retention (pretests) were administered anywhere from one semester to a year and a half later.
5. To determine if students completing remedial/developmental courses demonstrated similar achievement when compared to non-remedial/non-developmental students in the same course, data was analyzed as follows:
a) Algebra posttest scores achieved by former remedial students were compared, to algebra posttest scores achieved by students in the same developmental course (IM) who had been determined as not requiring a. remedial course based on the placement criteria and pretest results. :
b) Final grades in College Algebra achieved by former remedial/developmental students were compared to final grades achieved by non-remedial/non-development students in the same course in terms of the percent of students in each category sucdessfully, complete, the course. The College Algebra classes
were seleçed based on an enrollment of at least $10 \%$ former remedial/developmental students.

Statistical analysis of the data was carried out using Independent t-tests as no significant correlations were found between the scores being compared.

## Results.

The , results are presented according to the specifically stated oobjectives of the study.

With respect the first and second objective of the study, the findings showed that significant differences consistently existed between the pre-hnstructional skills assessment, as measured by pretest scores, and the post-instructional assessment, as measured by posttest scores, of students in the remedial andor developmental courses, over the three year period 198i-1984. Table $I$ shows the analysis. of the data by skill area, (computation and/or algebra), course (Basic Computational Math, remedial, Intro to Computational Math and Intro to Math, developmental), semester (Fall or Spring) and by. Academic Year (1981-82, 82-83, 83-84). Indeperident t-Lest analysis showed significant differences between pretest scores and posttest scores at .01 level in favor of the posttest scores in each skill area, for each "course, for each semester and each academic year. The results are clearly consistent over the three year period. Independent t-test analysis was used as there was no significant correlation between pretest scores and posttest scores.

COUPARISO!! OF PRETEST SCORES TO PGSTTEST SCORES BY
SHILL $\dot{A R E A}$, COITSE, SEEESER AND ACADEMIC VEAR



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Further, Table 2 shows the number and percent of students successfully completing the remedial and/or developmental courses for the entire 1981-1984 population. The success of the program is further supported by this data.

Table 2
SUCCESSFUL COMPLETION OF REMEDIAL AND DEVELOPMENTAL
COURSE ANALYSIS FOR ENTIRE 1981-84 POPULATION


* F grades were awarded to students who:
a) appeared on official enrollment roster but never attended class
b) did not pass the posttest
c) passed the posttests (24/30 correct) but did not adequately satisfy the course requirements.

Looking at the entire remedial/developmental population $\approx$ for the three year period 1981-1984, over $72 \%$ of the 324 scudents officially enrolled in the remedial course' (BCM) successfully completed it. Over $73 \%$ of 1,490 students officially enrolled in the developmental courses (ICM and IM) successfully completed it. It should be noted that according to college policy, $F$ grades were awarded to students whose names appeared on the official roster and who never
attended class. Approximately $7 \%$ of the F grades were awarded to students who never, attended class but appeared on the official grade roster. In addition, $F$ grades were awarded to students who may have passed the posttest with ai score of 24 out of 30 correct but who had not adequately. satisfied the other course requirements. Approximately $9 \%$ of the $F$ grades were awarded to students who passed the post test but failed the course. The remaining $F$ grades were awarded to students who did not pass the posttest with a score of 24 out of 30 correct. \&

For the third objective of the study, using the procedures and assumptions outlined in the Methods section, the findings indicated that the remedial/developmental program contributed significantly to the improvement of student mathematical skills. - Analysis of the data for 164 student; who first enrolled at- the college in Fall 1983, grouped according to those who enrolled in remedial/developmental courses in their first semester, Fall '83, and those who waited until their second semester, Spring ' 84 , to enroll in.remedial indoor developmental courses showed no significant differences between first semester and second semester placement scores, pretest scores or pastiest scores. Table 3A shows the analysis of this data by course. and skill area. Independent t-test analysis showed no significant differences between the two groups on the measures used, placement scores, pretest scores or post test scores.
, Table "3A

- 1

COMPARISON OFF PIACEMENI SCORES, PRETEST SCORES AND POSTTEST SCORES FOR FIRST SENESTER AND SECOND SEWESTER STUDENTS EY COURSE

1st Semester
Mean

2nd Semester
SD N.
$\mathrm{SD} \quad \mathrm{N} \quad$ Mear. $t$.

Placement Scores
BCM Computation
$11.385 \quad 4.102 \quad 18 \quad 11.276$
4.208
.085
IZM Computation
Algebra
$\begin{array}{llll}17.923 & 2.784 & 15 & 18.742\end{array}$
4.28537
.671
5.01

37
. 959
İ Computation
21.756
$4.054 \quad 28 \quad 22.104$
2.753

38
.409
Alge bra
11.968
5.680
$28 \quad 12.017$
5.566

38
$.035^{\circ}$
Pretest Scores
BCM Computation
ICM. Ccmputation
I:. Computation
$11.5 \quad 3.650^{\prime}$
$18 \quad 11.607$
4.524

28
.08

Algebra
18.85
11.66
2.503
$15 \quad 19 . \overline{567}$
4.324

37
.589
$15^{\circ}$ 9.75
4.929 • 37
.750
22.607
$28 \quad 27.342$
2.245

38
.949

Posttest Szares
STM Computation
IC. $A$ Computation Algebra
I. Computation

Aigebra

| 23.83 | 5.953 |
| :--- | :--- |
| 23.8 | 4.057 |
| 23.5 | 6.298 |
| 26.786 | 2.20 |
| 26.5 | 2.285 |

18
15
15
28
28
4.739
23.643
2.248

37
.222
24.0
4.133
.37
1.103
26.789
1.742

38
.006
-
12.886
5.727
$28 \quad 13.021$
5.086

38
.103

I.: | Algebra |
| :--- |
| Aigutation |
| Aigebra |

When first semester pretest scores were compared to first semester posttest scores, using independent t-test analysis, significant differences at the . 01 level were faund in favor of the post 5 sst scores. Independent t-test analysis also showed ignificant difference at the '01 level in favor of the posttest scores when second semester, pretest scores wert compared to. first semester posttest scores. The tivalus, for these pretest-posttest comparisons weré comparablef Table 3B shows the analysis of this data by course and skill area.

Table 3B
CaIPARISON $O F$ FIRST SEEESTER PRFTEST SC . 0 POSTTEST SCORES AND FIRST SENESTER POSTTEST SCORES TO SECON: $\therefore$ ISTER PRETEST SCORES


As there, were no significant differ -es in placement scores between the two groups, the first semester group and second semester group, the two groups were judged comparable in terms of their initial mathematical skill abilities. If factors" other than the program's activities, contributed significantly to improved student mathematical skills as measure $\chi^{\prime}$ by pretest scores and posttest scores then there should have been significant differences in favor of the second semester group when pretest and posttest scores were compared for the two groups. Further, the differences between first semester posttest scores and second semester pretest scores' should not have been as significant as the differences between first semester pretest scores and posttest scores. The results, however, as previously indicated, showed no significant differences between the first semester group and the second semester group. Therefore, dt was judged that the program contributed significantly to the improvement of student mathematical skills.

With respect, to the fourth objective of the study, the findings showed that students did retain a great deal of the content learned. There were significant differences in initial pretest scores in computation and algebra and respective retention test scores achieved at least one semester later. Independent t-test analysis showed significant differences at '. O1 level in favor of the retention test scores. Table 4 A shows the analysis of this data.

## Table 4A

COMPARISON OF INITIAL PRETEST SCORES TO RETENTION TEST SCORES

## Measure

Measure
Computation

Algebra

Pretest
-
Me an
21.458
10.091 $5.021 \quad 215$.
$5.021 \quad 115$.
『

* Significant at the . Ol level.

When posttest scores in computation and algebra were compared tó respective retention test scores, signficant differences at the . 01 level were found in favor of the posttest . 1 scores. Table 4 B shows the analysis of this data.

Table 4B
COMPARISON OF POSTTEST SCCRES AND
RETENTION TEST SCORES

| ise asure | Posttest |  |  | Retention Test |  |  |  |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
|  | Mean | SD | $N$ | Mean | SD | N | t |  |
| Computation | 25.152 | 4.363 | 85 | 22.021 | 4.883 | 85 | 4.40 | * |
| Al gebra | 26.686 | 2.925 | 115 | 21.251 | 5.698 | 115 | 8.37 | * |

* Significant at the . Cl level.
- Although the differences were statistically significant, the difference in posttest and retention test means in computation ( 25.152 vs.. 22.021) and algebra (26.286 vs. 21.251) had no practical significance. Further, when the retention test scores, which were the subsequent course (IM) pretest scores, for former remedial students were compared to the pretest scores of students placed directly into the developmental course (IM) no significant differences were found using independent. t-test analysis. Similarly when the retention test scores, the pretest scores for the College Algebra course l of former developmental. students were compared to the pretest scores of non-remedial/development students, no significant differences were found using indepenc it t-test analysis. Table 4 C shows the comparison of pretest scores for the aforementioned groups.

Table $4 C$
CaPARISON OF PRETEST SCORES BETVEEN FQRIIER REMEDIAL $\approx \mathrm{B} / \mathrm{OR}$ DEVELOPMENTAL STUDENTS AND NON REMEDIAL AND/ OR
DEVELOPMENTAL STUDENTS


For objective five, the findings showed that former remedial students did significantly better on the algebra posttest than did students placed directly into the developmental courses (IM or ICM). A comparison of algebra posttest scores between former remedial students and. students placed directly into the developmental course indicate *significant , differences at "the 01 level in favor of the scores achieved by former remedial students. The results of this analysis are presented in Table 5A.

Table 5A
COMPARISON OF POSTTEST SCORES IN ALGEBRA BETWEEN
FOR: ER FENIEDIAL STUDENTS AND NON-REMEDIAL STUDENTS


* Significant at the . 01 level
$\varepsilon$

Analysis of final grades achieved in College Algebra courses showed that $81 \%$ of the former remedial/developmental students successfully completed the college level mathematics course as compared to $80 \%$ of the non-remedial/developmental students. Table 5 B shows the final grade analysis and grade.

Table 5B
FINAL GRADE ANAIYSIS IN COLLEGE AIGEBRA COURSESFOR. FORMER REIEDIAL/DEVELOPMENTAL STUDENTS AND NON-RENEDIAL/NON-DEVELOPMENTAL STUDENTS

|  | N | Passing |  | Pefcent receiving grade of |  |  |  | Failing. |  | Withdrawal |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
|  |  | \# | 3 | A | B | C | D | \# | $\%$ | \# | $\%$ |
| Former <br> Remedial/ <br> Developraental <br> Students | 75 | 61 | 81\% | $7 \%$ | 27\% | $3 \times 6$ | 11\% $/$ | 7 | 9\% | $\checkmark$ | \% $\%$ |
| Non-remedial No:-developmerital students | 130 | 104 | 80\% | 20\% | 30\% | , ${ }^{21 \%}$ | - $9 \%$ | 10 | $8 \%^{\circ}$ | $\geq 6$ | 12\% |
| - |  |  |  |  |  |  |  |  | 1 | $\underline{\square}$ |  |

## Summary and Conclusions

The purpose of the study was to assess the effectiveness of the remedial/devel pmental mathematics program developed and implemented at Ramapo College of New Jersey. The results of the study show the program to be highly effective and highly successful in achieving the goals of mathematics remediation. Not only do the mathematical skill abilities of students enrolled in the program significantly improve as a result of the program's activities, but more importantly students successfully completing the program appear to have the same
opportunity for success in subsequent mathematics courses as do etudents not requiring remediation.

The results of this study have national implications for remedial/devȩlopmental mathematics instruction on the post-secondary level. In general, it provides concrete eviderce that remediation can achieve its objectives and that progra:ns can. be developed which significantly improve the mathematical skills performance of remedial/developmental students. In addition, given the statistically walidated ohigh degree of success of the Ramapo program, it can serve as gulde for other institutions of higher education which have not achieved the same degree of success. Successful mathematics remediation is not a luxury but a necessity since it increases the pool of potential students who opt for more mathematically or technically related fields, thereby filling a major demand in our society.


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